
CS688/WST665: Web-Scale Image Retrieval

Scale Invariant Region Selection

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Course URL:
<http://sglab.kaist.ac.kr/~sungeui/IR>

KAIST



What we will learn today?

- Local invariant features
 - Motivation
 - Requirements, invariances
- Keypoint localization
 - Harris corner detector
 - Hessian detector
- **Scale invariant region selection**
 - Automatic scale selection
 - Laplacian-of-Gaussian detector
 - Difference-of-Gaussian detector
 - Combinations
- Local descriptors
 - An intro

From Points to Regions...

- The Harris and Hessian operators define interest points.
 - Precise localization
 - High repeatability

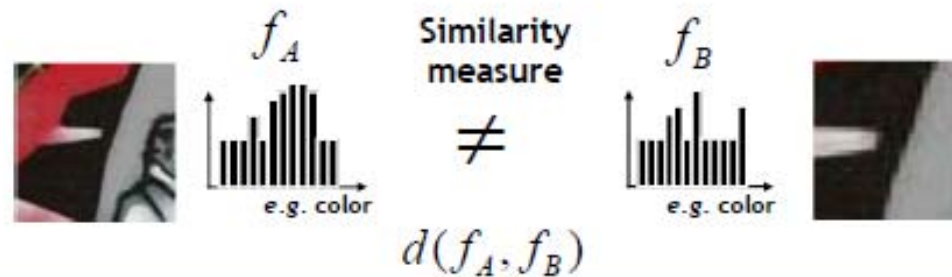


- In order to compare those points, we need to compute a descriptor over a region.
 - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*

Source: Bastian Leibe

Naïve Approach: Exhaustive Search

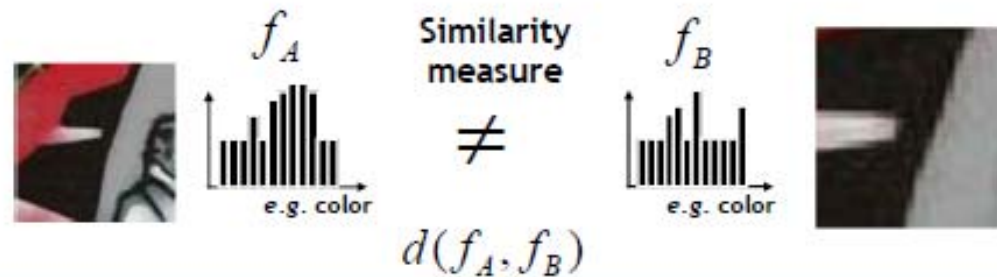
- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

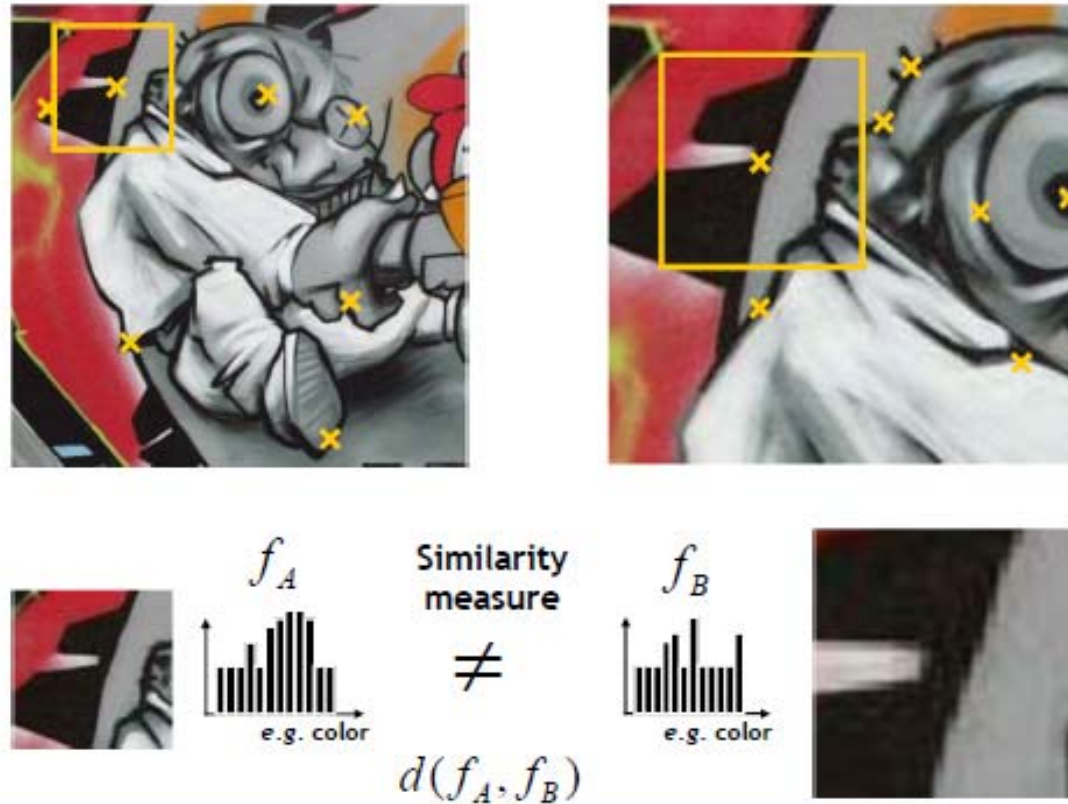
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Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

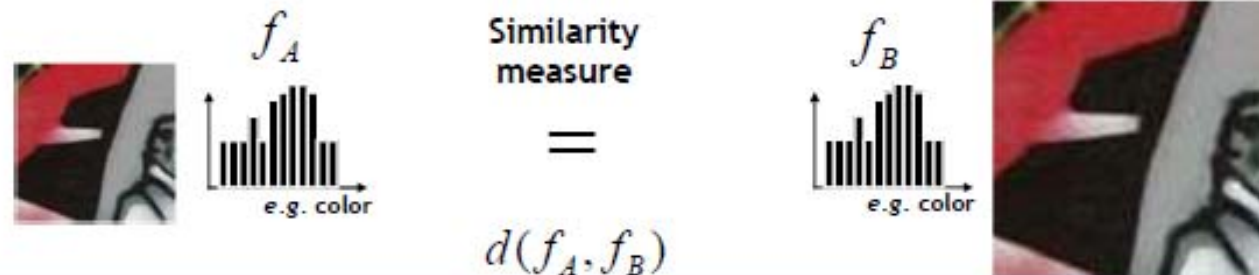
- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

- Comparing descriptors while varying the patch size
 - Computationally inefficient
 - Inefficient but possible for matching
 - Prohibitive for retrieval in large databases
 - Prohibitive for recognition



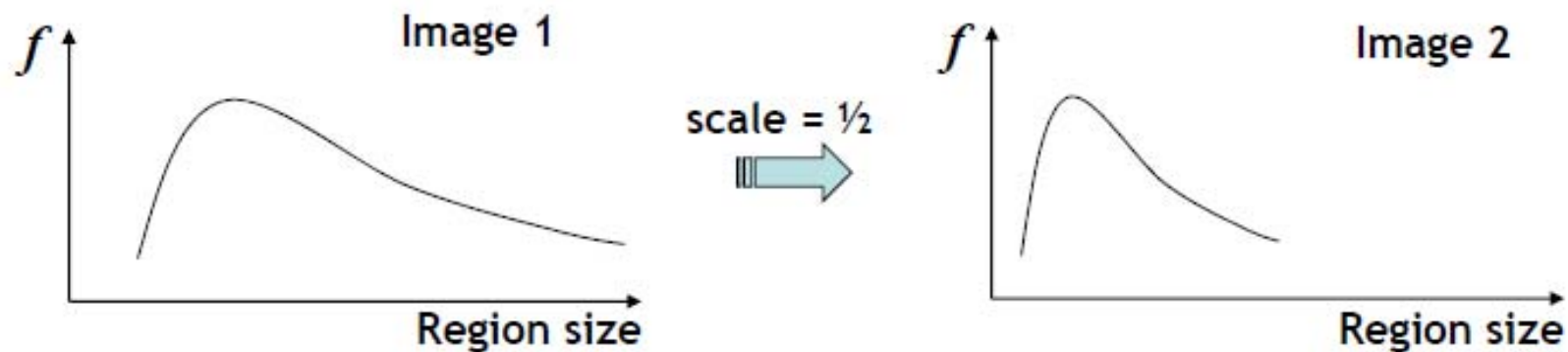
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Solution:
 - Design a function on the region, which is “scale invariant”
(the same for corresponding regions, even if they are at different scales)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

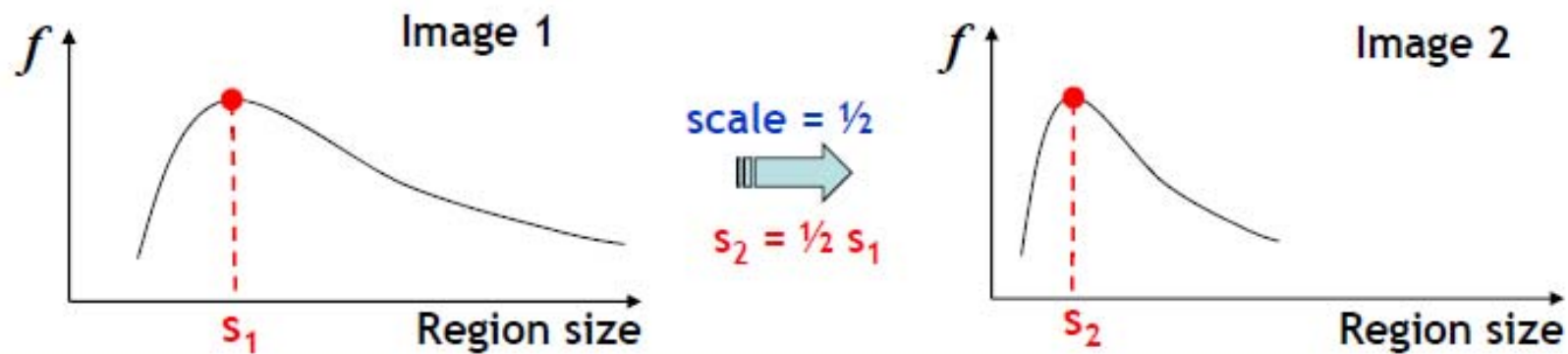
- For a point in one image, we can consider it as a function of region size (patch width)



Slide credit: Kristen Grauman

Automatic Scale Selection

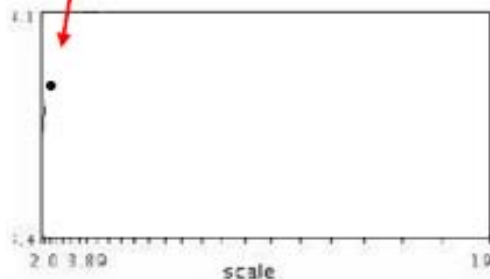
- Common approach:
 - Take a local maximum of this function.
 - Observation: region size for which the maximum is achieved should be *invariant* to image scale.



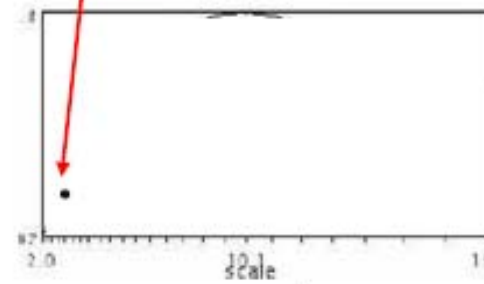
Slide credit: Kristen Grauman

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

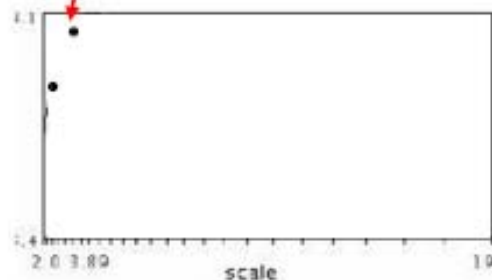


$$f(I_{i_1...i_m}(x', \sigma))$$

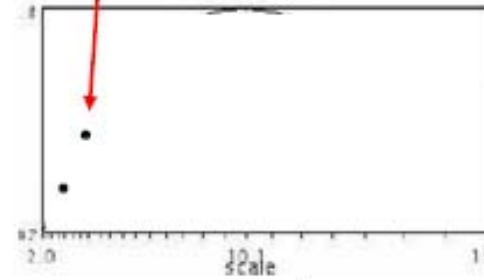
Slide credit: Krystian Mikolajczyk

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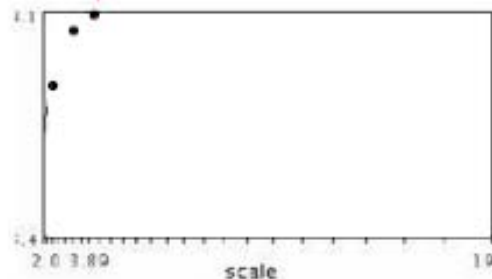


$$f(I_{i_1...i_m}(x', \sigma))$$

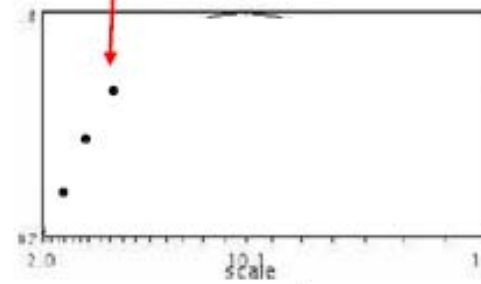
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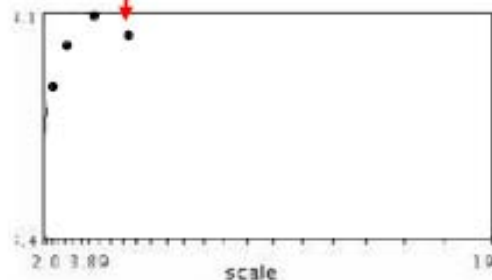


$$f(I_{i_1...i_m}(x', \sigma))$$

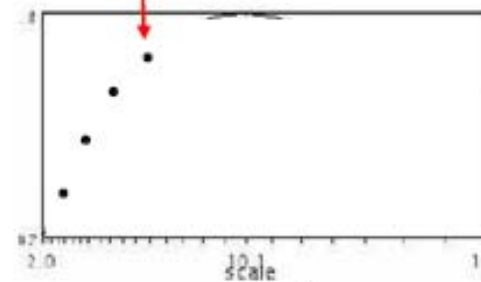
Slide credit: Krystian Mikolajczyk

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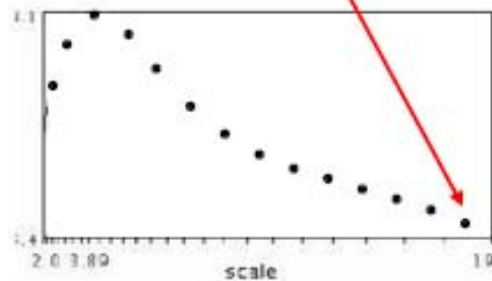


$$f(I_{i_1...i_m}(x', \sigma))$$

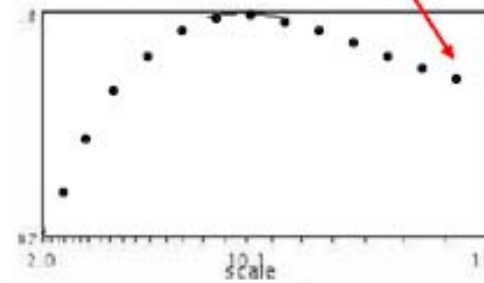
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

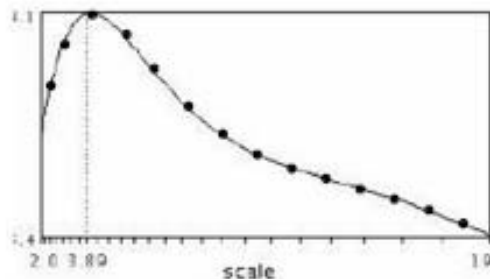


$$f(I_{i_1...i_m}(x', \sigma))$$

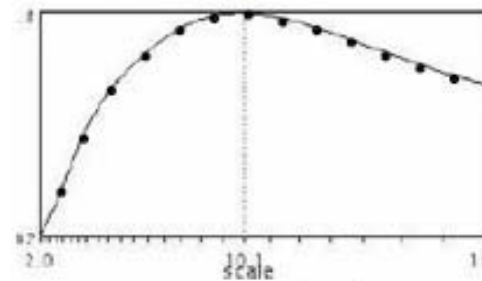
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

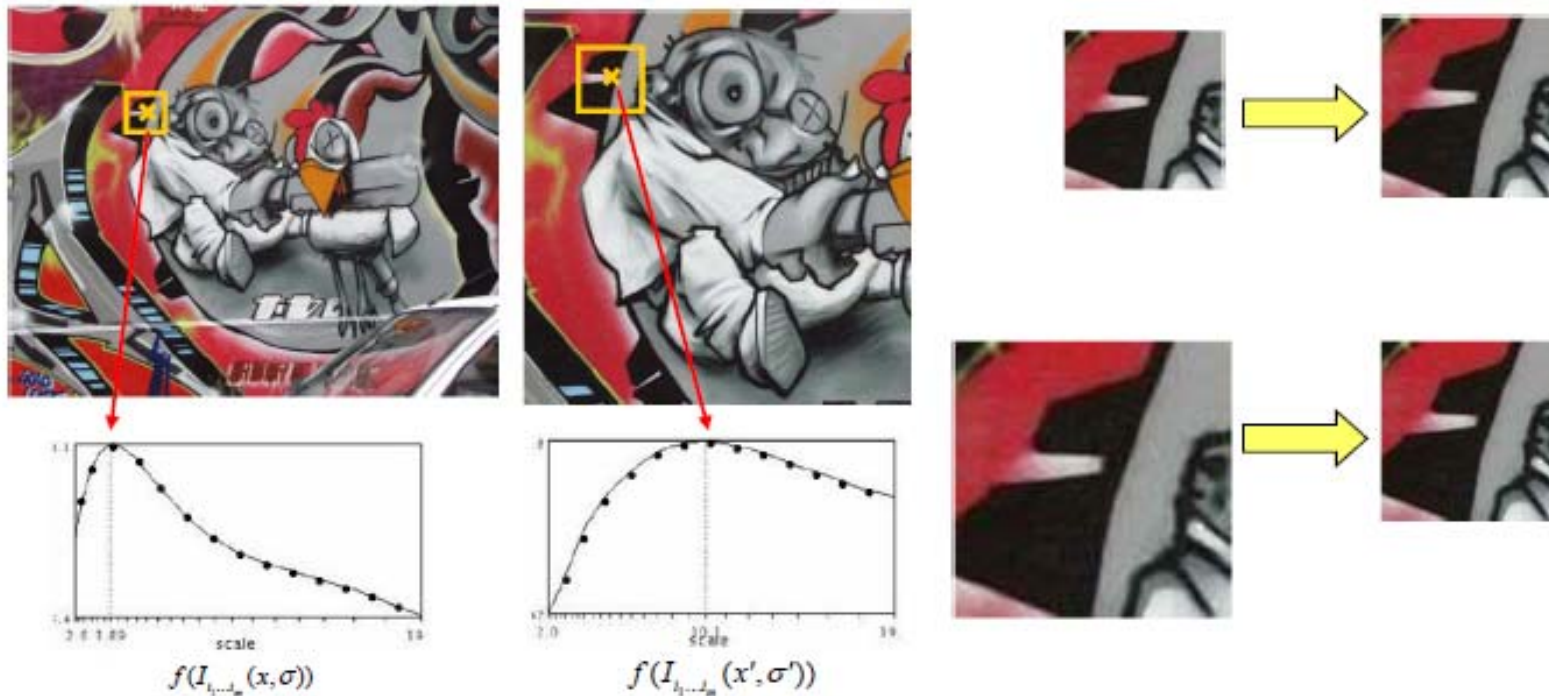


$$f(I_{i_1...i_m}(x', \sigma'))$$

Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

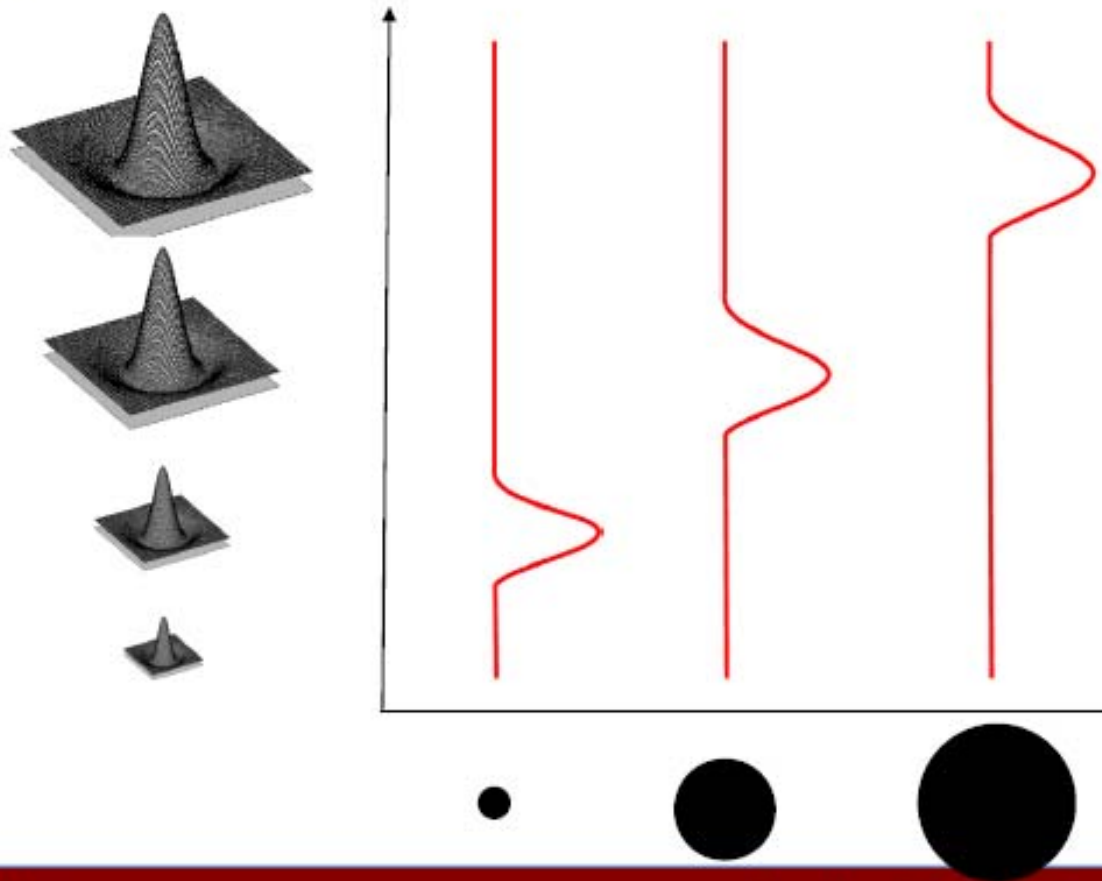
- Normalize: Rescale to fixed size



Slide credit: Tinne Tuytelaars

What Is A Useful Signature Function?

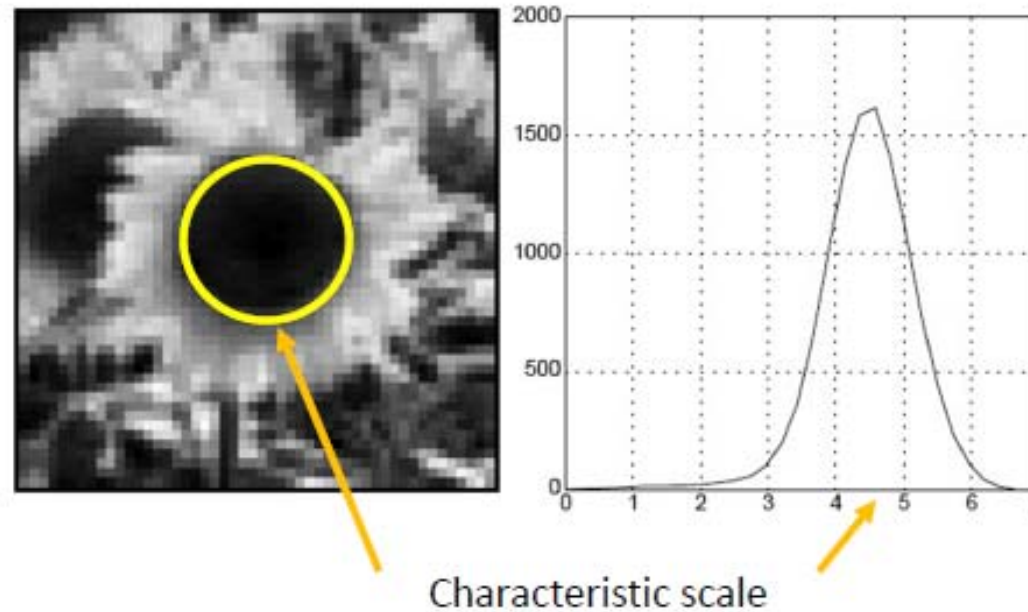
- Laplacian-of-Gaussian = “blob” detector



Slide credit: Bastian Leibe

Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response

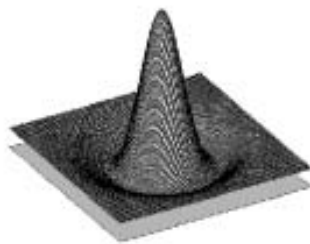


T. Lindeberg (1998). "[Feature detection with automatic scale selection.](#)" *International Journal of Computer Vision* 30 (2): pp 77–116.

Slide credit: Svetlana Lazebnik

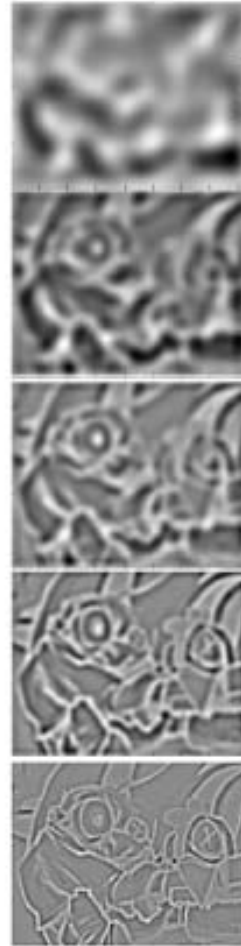
Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

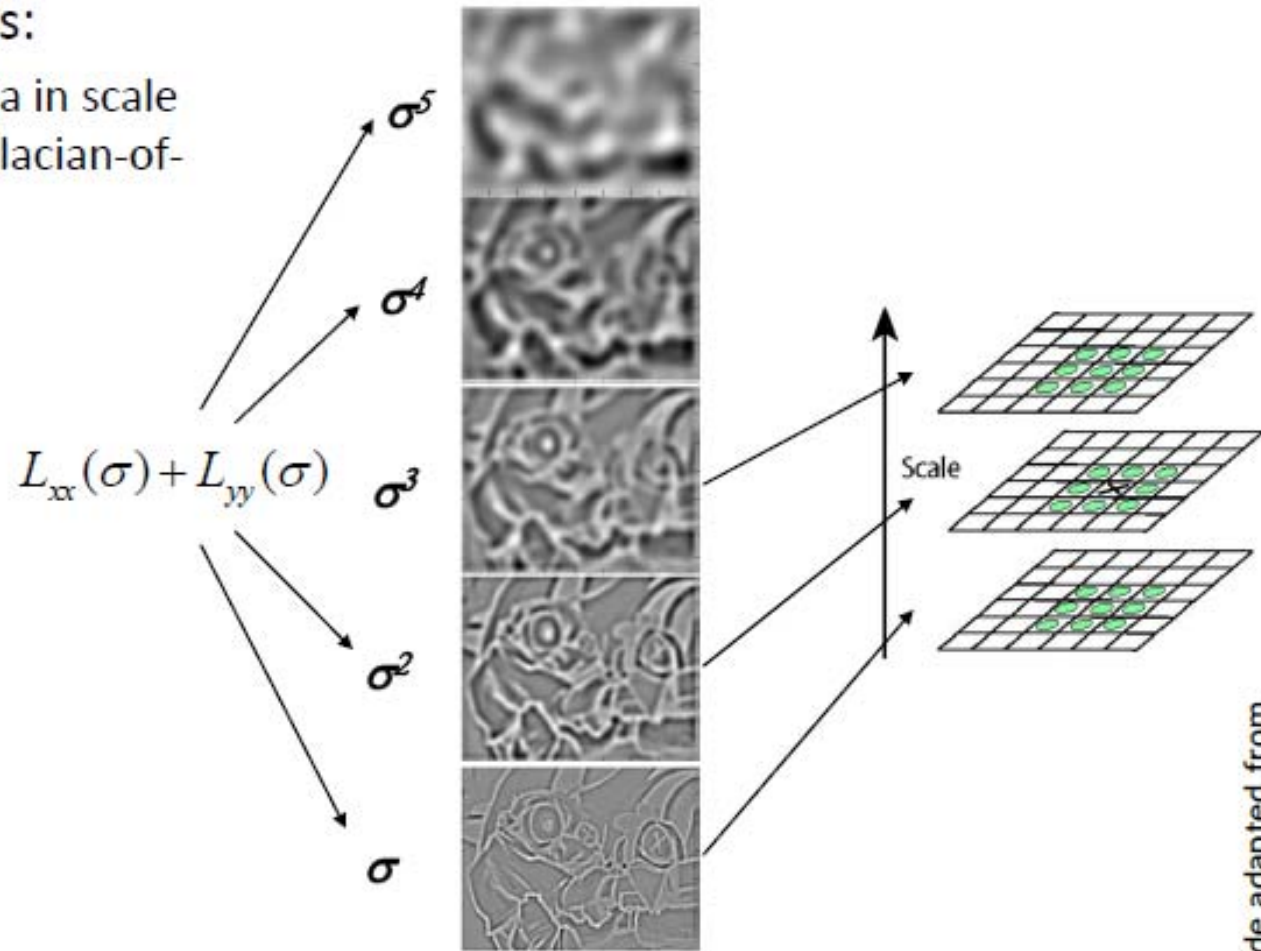
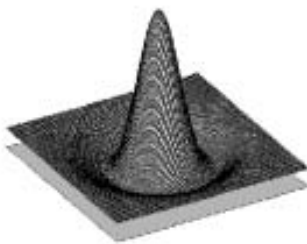
σ_5
 σ_4
 σ_3
 σ_2
 σ



Slide adapted from Krystian Mikolajczyk

Laplacian-of-Gaussian (LoG)

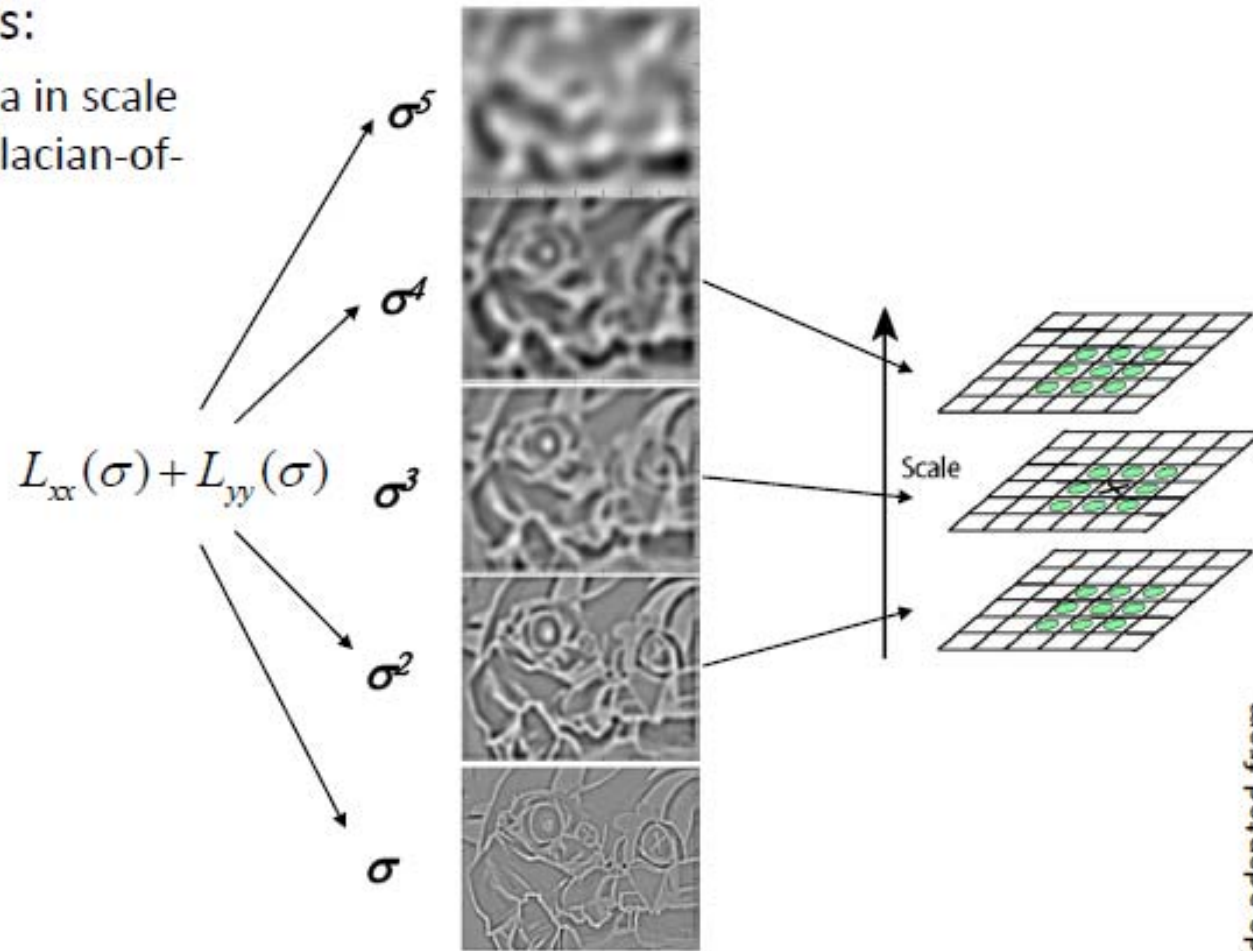
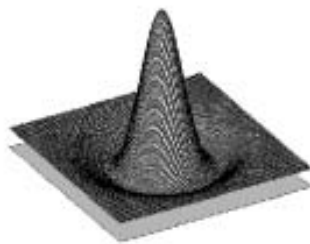
- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



Slide adapted from

Laplacian-of-Gaussian (LoG)

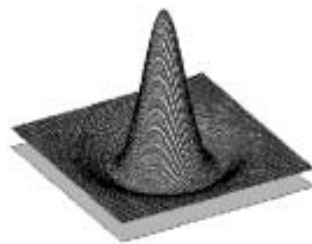
- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



Slide adapted from

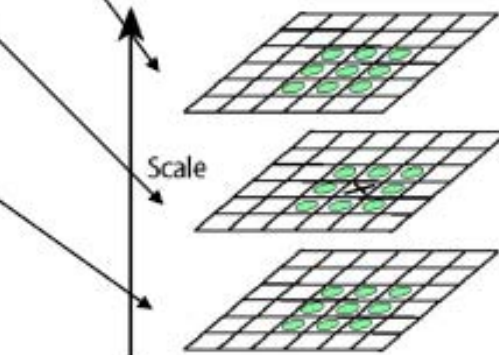
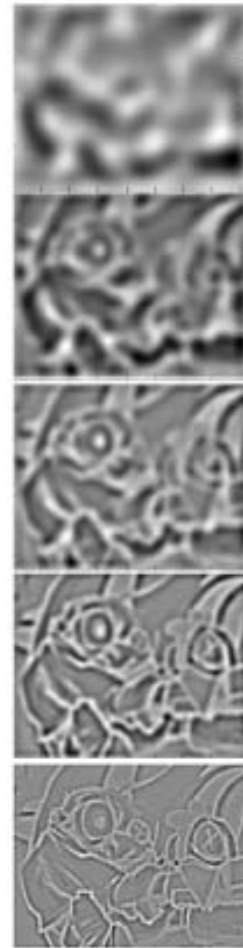
Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

σ_5
 σ_4
 σ_3
 σ_2
 σ



\Rightarrow List of (x, y, σ)

Slide adapted from

LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

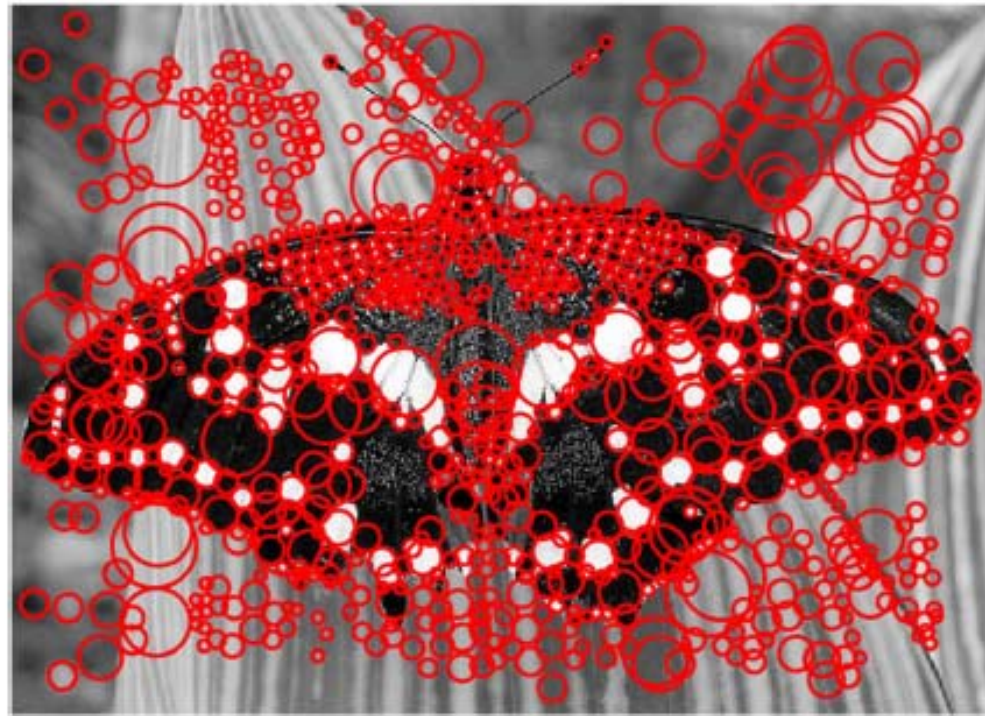
LoG Detector: Workflow



sigma = 11.9912

Slide credit: Svetlana Lazebnik

LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

Technical Detail

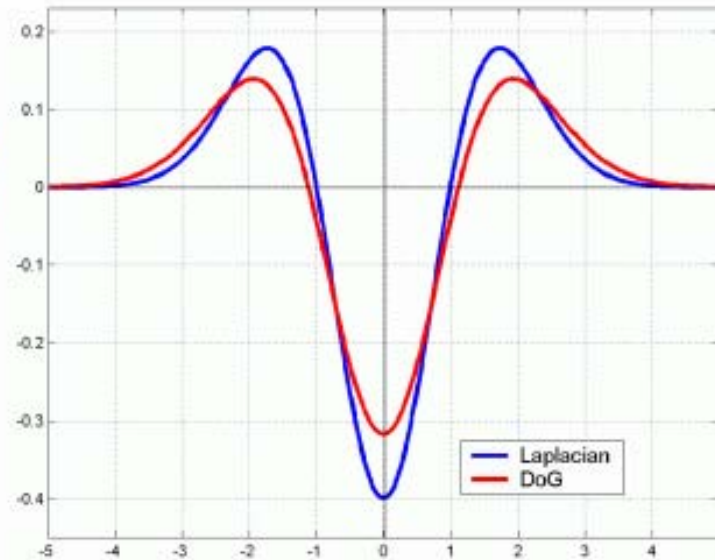
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 \left(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma) \right)$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

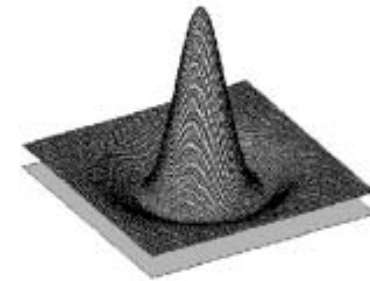
(Difference of Gaussians)



Slide credit: Bastian Leibe

Difference-of-Gaussian (DoG)

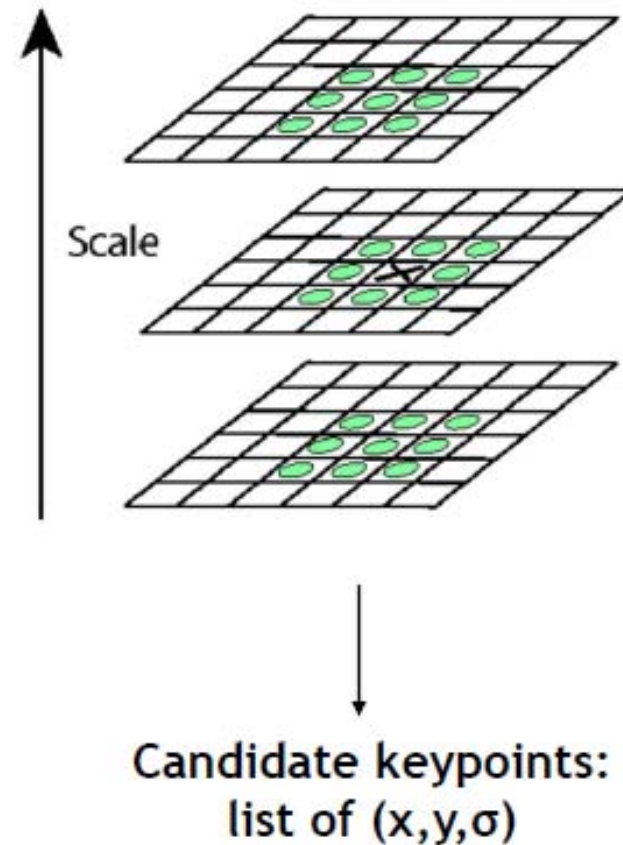
- Difference of Gaussians as approximation of the LoG
 - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
 - No need to compute 2nd derivatives
 - Gaussians are computed anyway, e.g. in a Gaussian pyramid.



Slide credit: Bastian Leibe

Key point localization with DoG

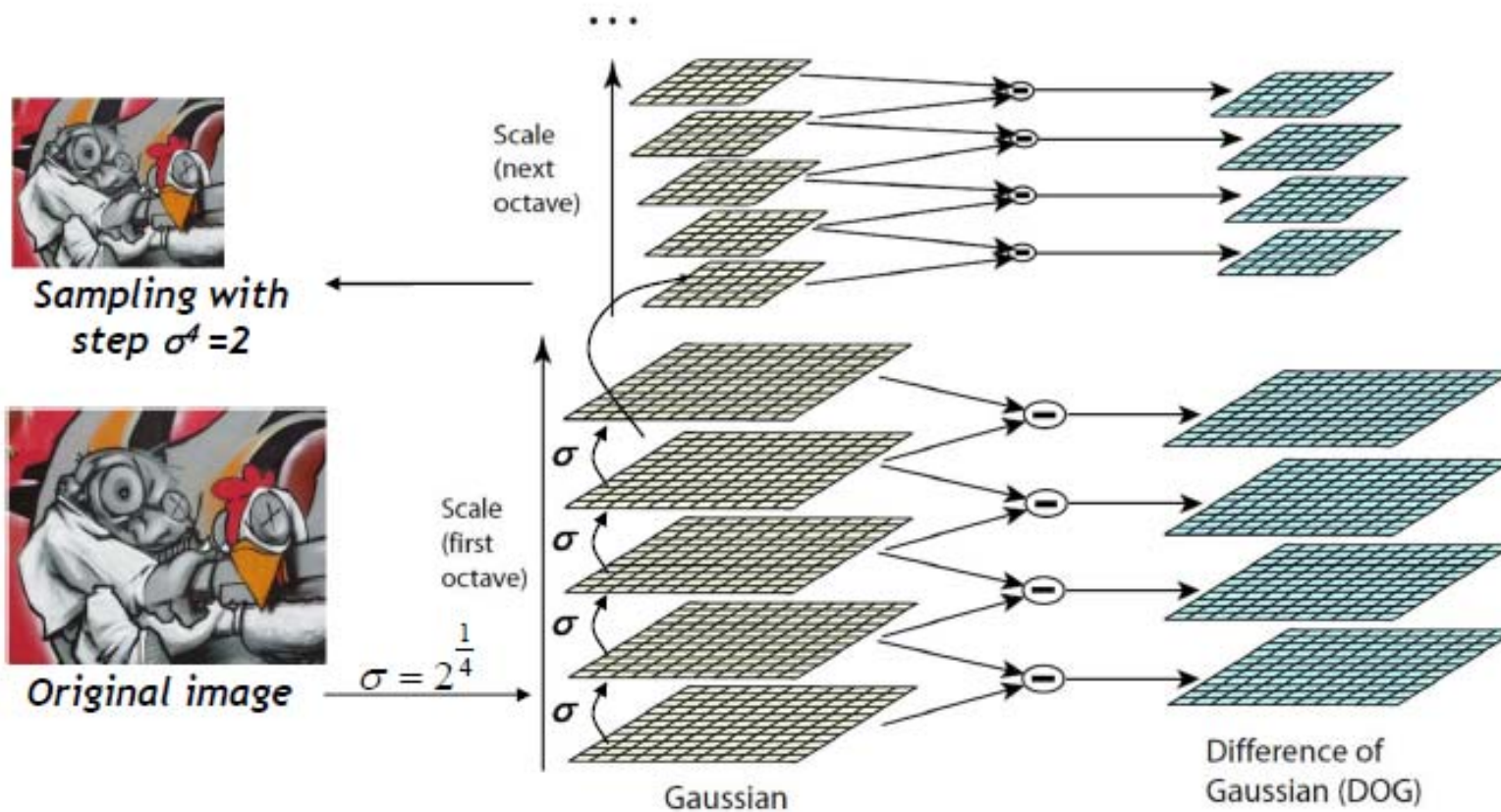
- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses



Slide credit: David Lowe

DoG – Efficient Computation

- Computation in Gaussian scale pyramid



Slide adapted from Krystian Mikolajczyk

Results: Lowe's DoG



Slide credit: Bastian Leibe

Example of Keypoint Detection



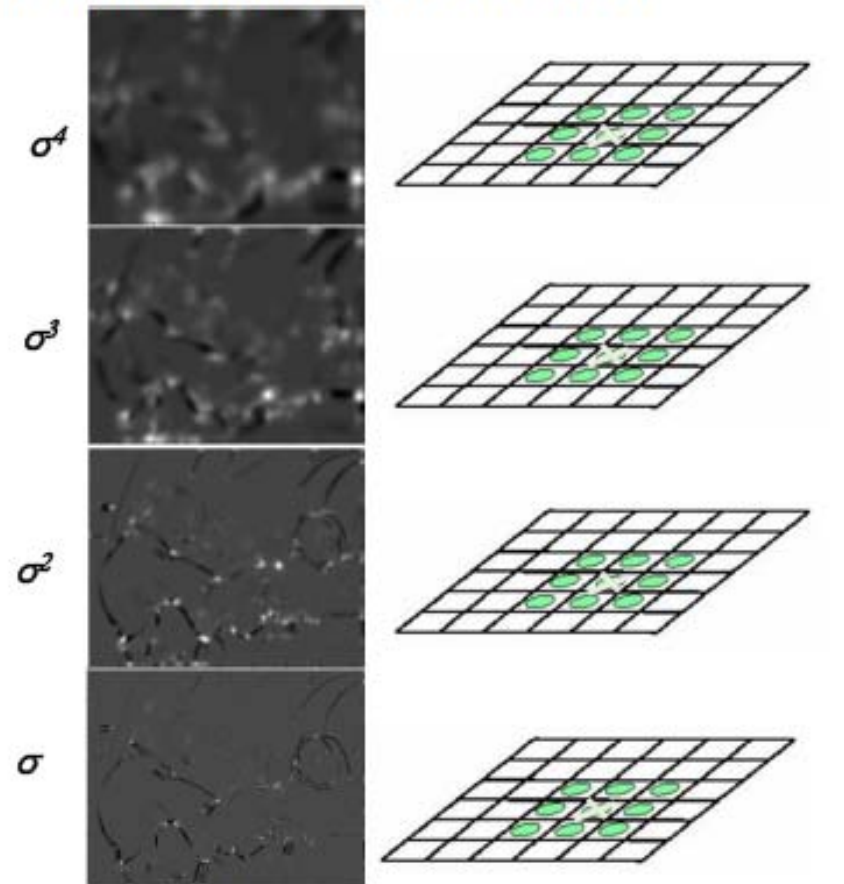
- (a) 233x189 image
- (b) 832 DoG extrema
- (c) 729 left after peak value threshold
- (d) 536 left after testing ratio of principle curvatures (removing edge responses)

Slide credit: David Lowe

Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection

Slide adapted from Krystian Mikolajczyk

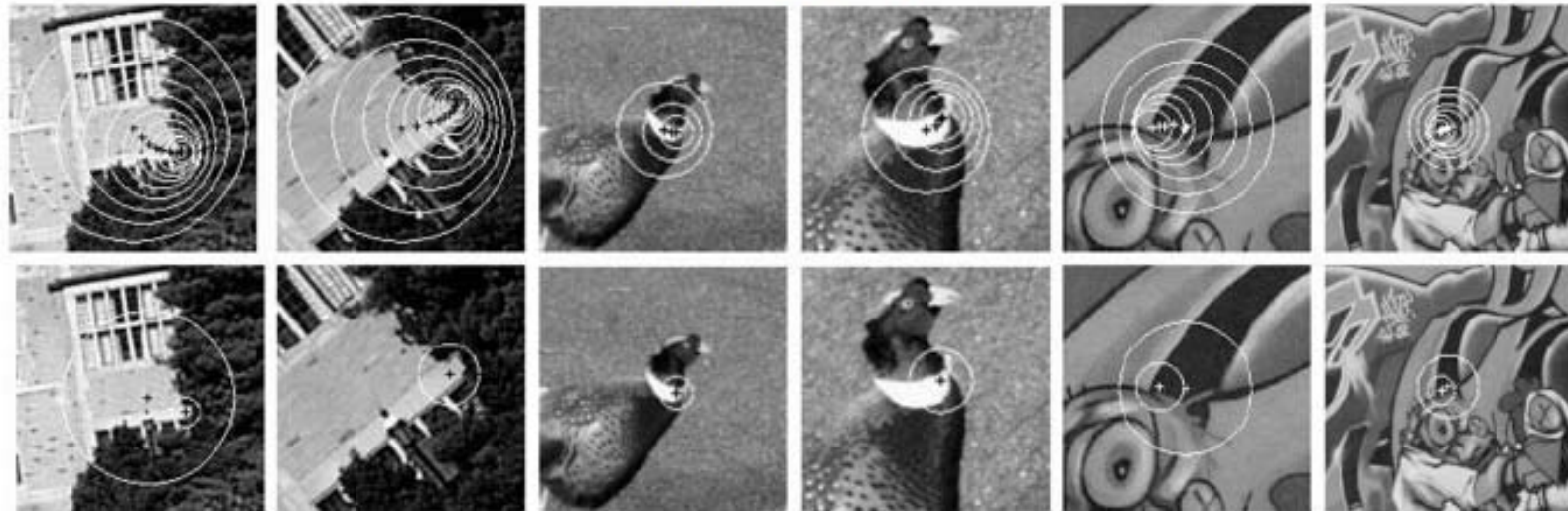


Computing Harris function Detecting local maxima

Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian
(same procedure with Hessian \Rightarrow Hessian-Laplace)

Harris points



Harris-Laplace points

Slide adapted from Krystian Mikolajczyk

Summary: Scale Invariant Detection

- **Given:** Two images of the same scene with a large *scale difference* between them.
- **Goal:** Find *the same* interest points *independently* in each image.
- **Solution:** Search for *maxima* of suitable functions in *scale* and in *space* (over the image).

- Two strategies
 - Laplacian-of-Gaussian (LoG)
 - Difference-of-Gaussian (DoG) as a fast approximation
 - *These can be used either on their own, or in combinations with single-scale keypoint detectors (Harris, Hessian).*

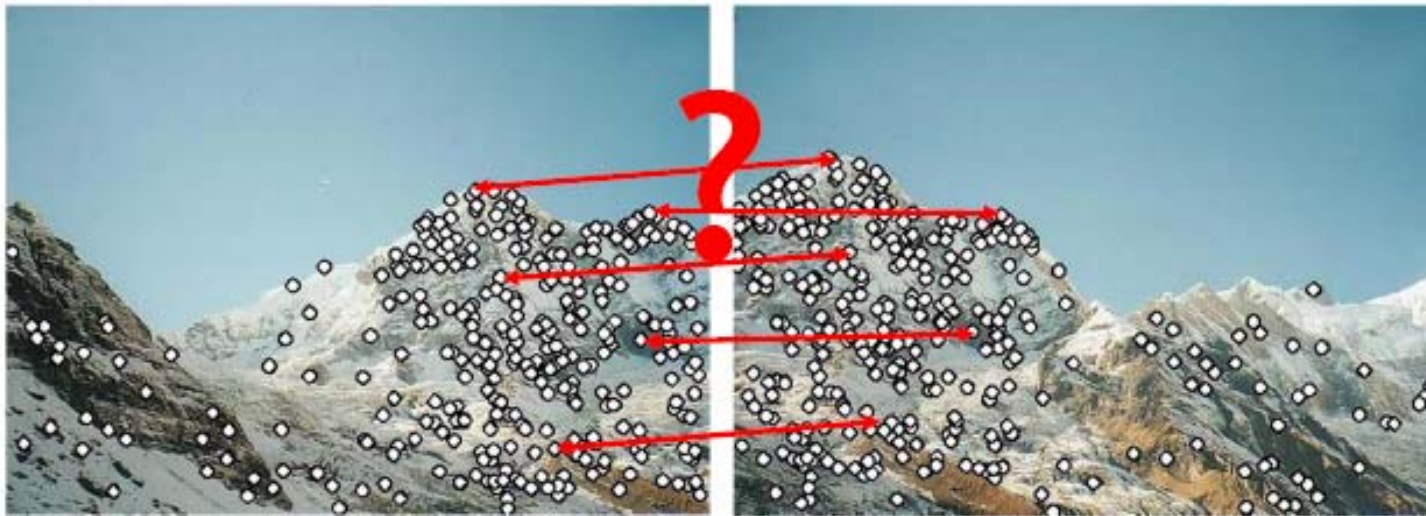
What we will learn today?

- Local invariant features
 - Motivation
 - Requirements, invariances
- Keypoint localization
 - Harris corner detector
 - Hessian detector
- Scale invariant region selection
 - Automatic scale selection
 - Laplacian-of-Gaussian detector
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 - Combinations
- Local descriptors
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Local Descriptors

- We know how to detect points
- Next question:

How to describe them for matching?



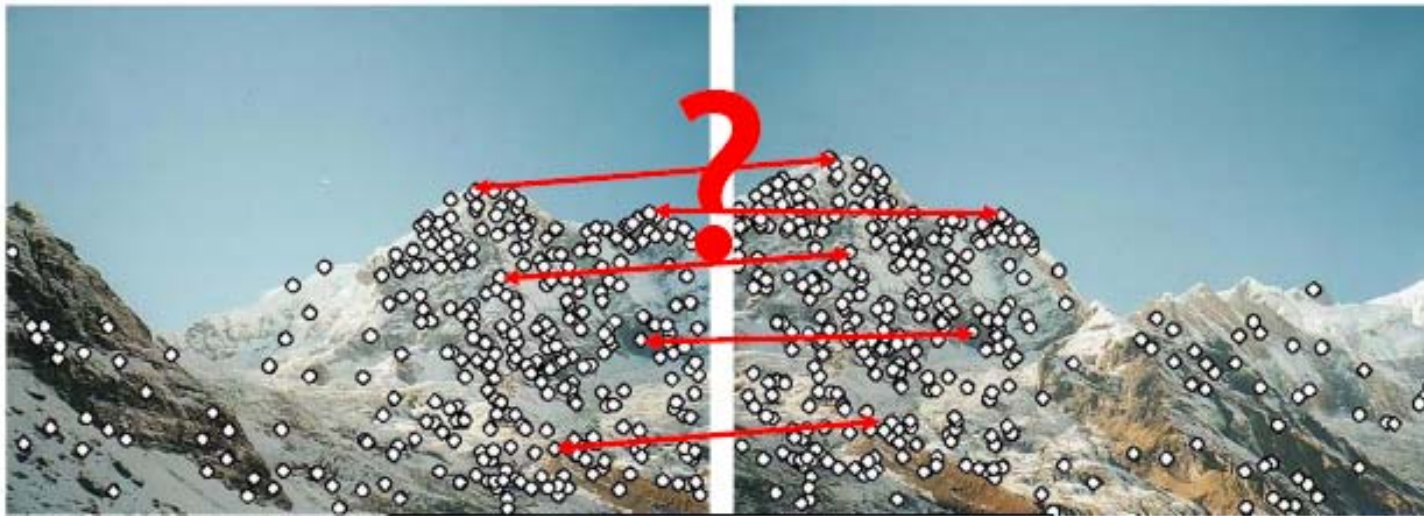
⇒ *Next lecture...*

Slide credit: Kristen Grauman

Local Descriptors

- We know how to detect points
- Next question:

How to describe them for matching?



Point descriptor should be:

1. Invariant
2. Distinctive

Slide credit: Kristen Grauman

Next Time

- Local descriptors (e.g., SIFT)

Homework for Every Class

- **Go over the next lecture slides**
- **Come up with one question on what we have discussed today**
 - 0 for no questions
 - 2 for typical questions
 - 3 for questions with thoughts
 - 4 for questions that surprised me